### MA 227, CALCULUS III Fall, 2010

Name (Print last name first):	 	 ••
Student Signature:	 	

# TEST 3

### 10 questions, 10 points each. SHOW ALL YOUR WORK!

<u>Question 1</u>

Find  $\int \int_D x \, dx \, dy$ , where D is bounded by  $y = x^4$  and y = 8x.

# <u>Question 2</u>

Find the volume under the surface  $z = x^2 y$  and above the triangle in the xy plane with vertices (0,0), (1,0), (1,1).

# <u>Question 3</u>

Sketch the region of integration and change the order of integration:

 $\int_0^1 \int_{x^4}^1 f(x,y) dy dx.$ 

# <u>Question 4</u>

Use polar coordinates to find the volume under the plane z = 2x + y + 8 and above the half-disk  $x^2 + y^2 \le 9$ ,  $x \ge 0$  in xy plane.

# $\underline{\text{Question } 5}$

Find the mass of the lamina that occupies the region:

$$D = \{(x, y) | x^2 + y^2 \le 1, y \ge 0\}$$

and has the density function given by  $\rho(x,y) = x^2 + y^2$ .

<u>Question 6</u>

Evaluate the iterated integral  $\int_0^1 dx \int_0^{x^2} dy \int_0^{x+y} dz$ .

 $\underline{\text{Question } 7}$ 

Express the integral  $\int \int \int_E f(x, y, z) dV$  as an iterated integral, where E is the solid above the region  $D = \{(x, y) : y^4 \le x \le 1\}$  in xy plane and below the plane z = x + y + 2.

### $\underline{\text{Question }8}$

Find  $\int \int_D (x+2y) dx dy$ , where D is bounded by x+2y=0, x+2y=4, x-y=0, x-y=2. Use change of variables u=x+2y, v=x-y.

#### $\underline{\text{Question }9}$

For the integral  $\int \int_D f(x,y) dxdy$  consider the change of variables u = xy,  $v = \frac{x}{y}$ . Find inverse change of variables x = x(u,v), y = y(u,v) and calculate corresponding Jacobian. You DO NOT need to substitute it into integral.

### <u>Question 10</u>

Using TWO DIFFERENT ITERATED INTEGRALS find area of the domain D bounded by  $y = x^2$ , y = 9. Be sure that you get the same answer in both cases.