CALCULUS II, TEST 1 MA 126 Closed Book, No Calculators

PART 1. Part 1 consists of 6 questions. Do your work and clearly write your answer in the space provided. No partial credit is awarded for this part of the test. (5 points each)

1. Find the equation of the plane that passes through P(-1,3,-2) and is parallel to the plane 2x - y + 4z = 7.

Answer: _____

- 2. Let $\vec{a} = <1,1,-1>$ and $\vec{b} = <3,-2,3>$. Find
 - (a) $comp_{\vec{a}}\vec{b}$

Answer: _____

(b) $proj_{\tilde{a}}b$

Answer:_____

3. Find the angle θ between the vectors $\vec{u} = \vec{i} + 2\vec{j} - 3\vec{k}$ and $\vec{v} = \vec{i} + \vec{j} + 2\vec{k}$. You may leave your answer in the form $\theta = \cos^{-1} y$.

Answer:_____

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4. A constant force $\vec{F} = 3\vec{i} + 5\vec{j} + 10\vec{k}$ moves an object along the line segment from the point P(1,0,1) to the point Q(5,3,8). Find the work done (include units) if the distance is measured in meters and the force in newtons.

Answer:_____

5. $16x^2 + 16y^2 + 16z^2 - 128x + 32y = 5$ is the equation of a sphere. Find the radius.

Answer:_____

6. Find the cross product of the vectors $\vec{u} = \langle 4, -6, 1 \rangle$ and $\vec{v} = \langle 1, -2, -2 \rangle$.

Answer:_____

<u>Part 2.</u> Part 2 consists of 5 problems worth 14 points apiece. Show all your work for full credit! Displaying only the final answer (even if correct) without the relevant steps is not enough.

Problem 1

This problem has two separate questions (a) and (b). Answer each question.

(a) Suppose two lines L_1, L_2 are given by the parametric equations given below. Determine whether these lines intersect. If they do intersect, find the point of intersection.

 $L_1: x = -1 + 2t, y = 3t, z = 4 - 3t$ $L_2: x = 3 + s, y = 1 - s, z = 1$

(b) Is the line given by $\vec{r} = <1,2,3 > + t < -2,2,-4 >$ parallel to the line given by $\vec{r} = <-1,3,-4 > + t < 1,-1,8 >$ Why or why not?

Let P(1,4,6), Q(-2,5,-1), and R(1,-1,1) be three points in R^3 .

(a) Find the equation of the plane through the points P,Q, and R.

(b) Find the area of ΔPQR , the triangle with vertices at P, Q, and R.

(a) Find the parametric equations and symmetric equations for the line L. Label which is which.

(b) At what point does this line intersect the xy – plane?

Let x + y - z = 2 and 2x - y + 3z = 1 be the equation of two planes.

(a) Find one point that lies on the line of intersection of the two planes.

(b) Find the vector equation of the line of intersection of the two planes.

A particle is traveling along the space curve

$$\vec{r} = \left\langle \frac{2t+1}{t}, e^{-t}, \frac{\ln t}{t} \right\rangle$$

for time t where t > 0.

(a) Evaluate $\lim_{t\to\infty} \vec{r}(t)$ to see what point the particle approaches after a long time.

(b) Determine a unit tangent vector to the curve at the pint where t = 1.

Extra Credit Problem (10 points)

Find the distance between the point P(2,8,5) and the plane given by x-2y-2z=1.