# Calculus 2

## MA126-8B

## Midterm Examination 1

# Tuesday, September 30, 2003

**Instruction:** Answer the questions in the space provided. Use the scratch paper provided if needed. Please keep your answers neat, brief, and to the point. Show all the steps in your derivations.

Question 1	
Question 2	
Question 3	
Question 4	
Question 5	
Question 6	
Total	
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**QUESTION 1.** Define:

$$f(x) = \int_0^x \sin(t^2) dt, \qquad -\sqrt{\pi} < x < \sqrt{\pi}.$$

Determine the interval(s) where f is decreasing.

**QUESTION 2.** Find the integral:

$$\int \frac{dx}{\sqrt{x^2 - 4}}.$$

*Hint:* Substitute  $x = 2 \cosh u$ .

**QUESTION 3.** Find the integral:

 $\int (\ln x)^2 \, dx.$ 

**QUESTION 4.** Compute:

$$\int_0^1 \frac{x^3 \, dx}{x^2 + 1}.$$

**QUESTION 5.** The trapezoid method  $T_n$  is used to approximate the following integral:

$$\int_0^1 \cos\left(x^3\right) \, dx.$$

How large should one choose n in order to guarantee the error is less than  $10^{-6}$ ? *Hint:* Recall that the error in the trapezoid method can be estimated by:

$$|E_M| \le \frac{K(b-a)^3}{12n^2}.$$

**QUESTION 6.** Determine whether the following improper integral converges:

$$\int_0^1 \frac{\sqrt{x^2 + 1}}{x} \, dx.$$